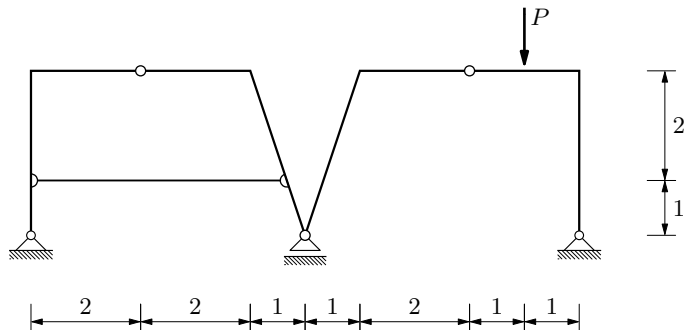


GS 1. — 1. kolokvij (B) (2023./2024.)

Zadatak 2.

Nacrtajte dijagrame unutarnjih sila!

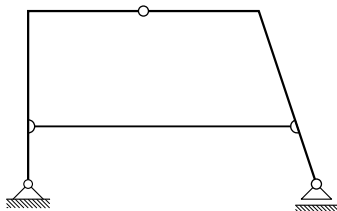
$$P = 100 \text{ kN}$$



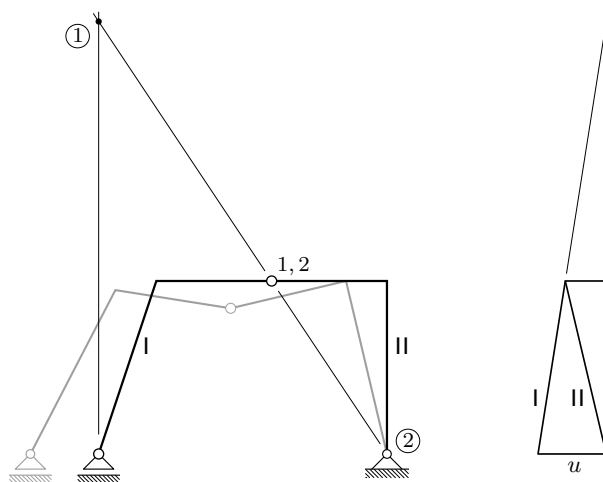
(Za potpuniju i detaljniju priču pročitajte primjer rješavanja istovrsnoga sistema — trozglobnoga nosača koji se „oslanja” na trozglobni nosač sa zategom — u datoteci <http://master.grad.hr/nastava/gS/gS1/isp/1-220906-2.pdf>, dostupnoj na stranici s bilješkama s predavanja (<http://master.grad.hr/nastava/gS/gS1/>.)

prepoznavanje statičkoga sistema: složeni ulančeni sistem

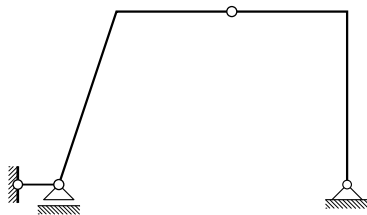
„temeljni” podsistem: lijevi podsistem — trozglobni nosač sa zategom:



desni podsistem bez lijevoga podsistema — mehanizam:



desni podsistem slijeva „temeljen” na lijevom podsistemu — trozglobni nosač:



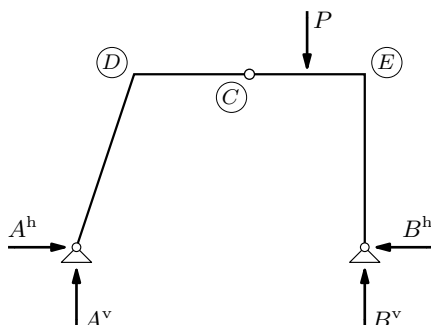
redosljed rješavanja:

reakcije trozglobnoga nosača → opterećenje trozglobnoga nosača sa zategom

⇒ (1) trozglobni nosač pa (2) trozglobni nosač sa zategom

(1) trozglobni nosač:

vrijednosti reakcija:



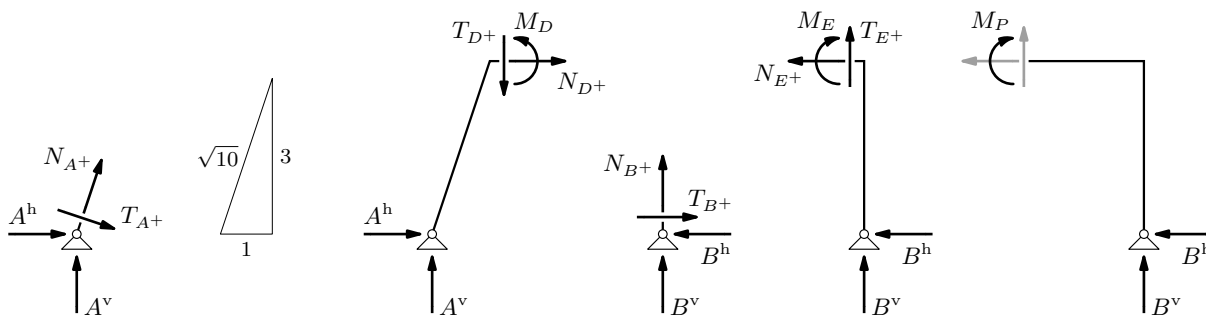
$$\sum_{\widehat{AB}} M_{/B} = 0 : \quad -5 \cdot A^v + 1 \cdot P = 0 \quad \Rightarrow \quad A^v = \frac{P}{5} = 20 \text{ kN}$$

$$\sum_{\widehat{AB}} M_{/A} = 0 : \quad -4 \cdot P + 5 \cdot B^v = 0 \quad \Rightarrow \quad B^v = \frac{4 \cdot P}{5} = 80 \text{ kN}$$

$$\sum_{\widehat{AC}} M_{/C} = 0 : \quad -3 \cdot A^v + 3 \cdot A^h = 0 \quad \Rightarrow \quad A^h = A^v = 20 \text{ kN}$$

$$\sum_{\widehat{AB}} F_x = 0 : \quad A^h - B^h = 0 \quad \Rightarrow \quad B^h = A^h = 20 \text{ kN}$$

vrijednosti unutarnjih sila:

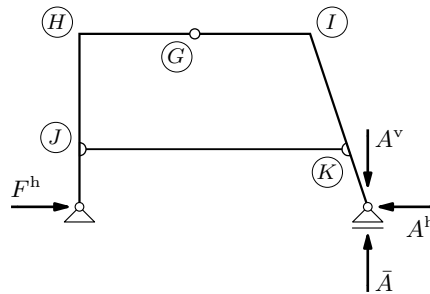


$$\sum_{\widehat{AD}} M_{/D} = 0 : \quad 3 \cdot A^h - 1 \cdot A^v + M_D = 0 \quad \Rightarrow \quad M_D = -40 \text{ kNm}$$

$$\begin{aligned} \sum_{\widehat{BE}} M_{/E} = 0 : \quad & -3 \cdot B^h - M_E = 0 \quad \Rightarrow \quad M_E = -60 \text{ kNm} \\ \sum_{\widehat{BP}} M_{/P} = 0 : \quad & -3 \cdot B^h + 1 \cdot B^h - M_P = 0 \quad \Rightarrow \quad M_P = 20 \text{ kNm} \\ \left. \begin{aligned} \sum_{A^+} F_x = 0 : \quad & \frac{1}{\sqrt{10}} N_{A^+} + \frac{3}{\sqrt{10}} T_{A^+} + A^h = 0 \\ \sum_{A^+} F_z = 0 : \quad & -\frac{3}{\sqrt{10}} N_{A^+} + \frac{1}{\sqrt{10}} T_{A^+} - A^v = 0 \end{aligned} \right\} \begin{aligned} N_{A^+} &= -8\sqrt{10} \text{ kN} \\ T_{A^+} &= -4\sqrt{10} \text{ kN} \end{aligned} \\ \sum_{B^+} F_x = 0 : \quad & -B^h + T_{B^+} = 0 \quad \Rightarrow \quad T_{B^+} = B^h = 20 \text{ kN} \\ \sum_{B^+} F_z = 0 : \quad & -B^v - N_{B^+} = 0 \quad \Rightarrow \quad N_{B^+} = -B^v = -80 \text{ kN} \\ \sum_{D^+} F_x = 0 : \quad & A^h + N_{D^+} = 0 \quad \Rightarrow \quad N_{D^+} = -A^h = -20 \text{ kN} \\ \sum_{D^+} F_z = 0 : \quad & -A^v + T_{D^+} = 0 \quad \Rightarrow \quad T_{D^+} = A^v = 20 \text{ kN} \\ \sum_{E^+} F_x = 0 : \quad & -B^h - N_{E^+} = 0 \quad \Rightarrow \quad N_{E^+} = -B^h = -20 \text{ kN} \\ \sum_{E^+} F_z = 0 : \quad & -B^v - T_{E^+} = 0 \quad \Rightarrow \quad T_{E^+} = -B^v = -80 \text{ kN} \end{aligned}$$

(2) trozglobni nosač sa zategom:

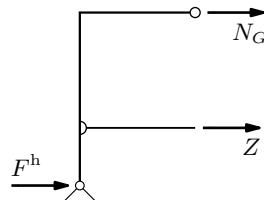
vrijednosti reakcija:



$$F^h = A^h = 20 \text{ kN}$$

$$\bar{A} = A^v = 20 \text{ kN} \quad \& \quad F^v = 0$$

vrijednost sile u zategi:



$$\sum_{\widehat{FG}} M_{/G} = 0 : \quad 3 \cdot F^h + 2 \cdot Z = 0 \quad \Rightarrow \quad Z = -\frac{3}{2} \cdot F^h = -30 \text{ kN}$$

$$\sum_{\widehat{FG}} F_x = 0 : \quad F^h + Z + N_G = 0 \quad \Rightarrow \quad N_G = -F^h - Z = 10 \text{ kN}$$

vrijednosti ostalih unutarnjih sila:

$$M_J = -1 \cdot F^h = -20 \text{ kN}$$

$$M_K = 1 \cdot A^h = 20 \text{ kN}$$

$$T_{F^+} = -F^h = -20 \text{ kN}$$

$$T_{H^-} = N_G = 10 \text{ kN}$$

$$T_{\bar{A}^+} = \frac{3}{\sqrt{10}} A^h = 6\sqrt{10} \text{ kN}$$

$$N_{\bar{A}^+} = -\frac{1}{\sqrt{10}} A^h = -2\sqrt{10} \text{ kN}$$

$$T_{I^-} = -\frac{3}{\sqrt{10}} N_G = -3\sqrt{10} \text{ kN}$$

$$N_{I^-} = \frac{1}{\sqrt{10}} N_G = \sqrt{10} \text{ kN}$$

dijagrami:

